### **STRUCTURAL PERFORMANCE OF STADIUM WITH THIN SHELL ROOF STRUCTURE**

**Prof. Dr. Govinda Prasad Lamichhane\*; Er. Raja Ram Chaudhary\*\***

\*Professor, School of Engineering, Pokhara University, Kaski, NEPAL

\*\* School of Engineering, Mid-West University, Birendra Nagar, Surkhet, NEPAL

**DOI: 10.5958/2278-4853.2023.00044.7**

#### **ABSTRACT**

*Structural Engineers and Architects Focused on Shell Structures because of Aesthetic Concerns and their ability to cover large spans also in Extreme condition such as Earthquakes and Hurricanes. In this thesis, Analysis of dome form, Para sine form and Mongue's Surface of Thin Shell Roof Structure in stadium are analysed. Deflection, Moment, Stress variation are analysed based on with Bracing and uniform thickness of shell, Without Bracing and uniform thickness of shell, with bracing and varying thickness of shell and without bracing and varying thickness of shell. For the comparison propose and to observe effect of edge and mesh fineness, dome is modeled as an axi-symmetric model and two axi-symmetric load i.e. self-weight and Seismic Loads are applied to the dome roof in SAP 2000. With Bracing and uniform thickness of slab, Without Bracing and uniform thickness of shell, with bracing and varying thickness of shell and without bracing and varying thickness of shell Roof Structure in Stadium is compared.* 

#### **KEYWORDS**: *Dome, Parabolic Sinusoidal Curve, Bracing Etc.*

#### **INTRODUCTION**

The development and construction of thin concrete shell structures dates back to the early 1920's when modern architecture looked for new curvilinear type of free forms of long span, thin, and economical ways to build roof structures that would cover large assembly places, sports arenas, public markets, music halls, and some other similar outdoor and indoor spaces where large number of people could gather under a solid and sound roof structure. Shell structures are very interesting due to their impressive strength-to-weight ratios. They are able to span over large areas, while having an exceptionally less thickness. This is primarily due to their form based structural behavior. The shells earthquake resistance is determined directly by performing a response spectrum analysis, but also indirectly by evaluating the fundamental frequencies of the shell structures. The eigen values and corresponding Eigen modes of a shell are solely dependent on the shell's stiffness and mass distribution, and thus, are independent of loading. Because of difficult to construction, analysis and of shell structure, scope of the shell structure was not come

A peer reviewed journal

in more practice before 1960's period (1). After some decade development of the computer, numerical method like finite difference method, finite element method etc and development of the new technology of construction, scope of the shell structure start to rise due to aesthetic and structural point of view as impressive strength-to-weight ratios.

We see in shell structure a conventional type of the geometry is used in the field of research and construction example cylindrical shell, conical shell, paraboloid shell, hyperbolic-paraboloid shell etc. with the uniform thickness with or without edge beam. the purpose of this thesis is to use complex geometry like mongue carved surface structure to increase the field of research and to find the best approach geometry for construction of the roof structure keeping good aesthetics appearance and to see /analyse the thin shell roof with the different loading conditions example static, dynamic loading condition etc. Carved surfaces were first studied by the French mathematician-geometer Mongue Gaspard (1746-1818). A carved Mongue surface is a surface composed of orthogonal trajectories of a one-parameter family of planes. Juhanio M. A. was the first researcher who attempts to find the strength of shell in the form of carved Mongue's surface.

Simply Supported Shells (20):- The Term "Simply Supported Shells" describes shells, which terminate at transverse stiffeners that must be integral with the shell. Shell continuous over the stiffeners ate designated as "continuous Shells".

Shells Continuous Over Supports. -The effect of continuity over the supports on stresses in shells is similar to the effect of continuity on stresses in ordinary beams. End restraint of the shell by continuity creates longitudinal stresses at the support, whose magnitude (and sign) are approximately in the same ratio to the longitudinal stresses in the simply supported shell as the end moments in a continuous beam are to the positive (middle span) moment in the same beam, simply supported. In some cases, the values obtained by a rigorous satisfaction of the boundary conditions and those obtained by proportioning the internal forces based on the ratio of end moments to the moment in a simply supported beam are practically identical.

#### **RESEARCH ANALYSIS:**

Most of the thin shell roof structure is analysed based on the use of dead load and live load, which might be seen unsafe in Seismic load on structural system. So in this thesis we are going to use varied thickness on the basis of only live load, dead load stress distribution but we are taking in to account as Seismic load. Seismic load in the thin shell structure as roof of the stadium, the roof can bear the Seismic load edge beam of the structure to transfer the stress of one component to the other component or to prevent the edge of the support from punching. Similarly, we can see normally research on simple geometry form so to increase field of research, this thesis aim is to analyse the complex shell roof dynamically and statically by using latest advanced analysis method. The problem induced in the structure as buckling and stress concentration are normally prevented by using bracing which help to transfer stress.

- $\checkmark$  Every part of the roof, the stress due to loads induced and the stress is concentrate at the intersection of the roof as edge beam, we should analyse the structure by different method of analysis.
- Analysis of dome structure, Para sine form structure.

ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 A peer reviewed journal

Different tools are used to analysis and of the structure. This first work while starting research is modeling in Sap 2000, Fortran etc. programming for the analysis, validation with manual sectored/discrete form and use of elastic theory, and seismic performance of shell roof Superstructure in Two consecutive direction with validation.



#### **TABLE 1: DETAILING OF STADIUM**

To create sample example of para sine detailed analysis in FORTRAN

**Script of FORTRAN built in program for carved mongue's surface: -**

NUMBER 0F PACES ALONG AXE X1 - 40 NUMBER OF PACES ALONG AXE X2 - 60 KUS= 8127

E=0.27000E+08 HU= 0.150 ALPHA0= -15.000 BITA0= .000 H=0.25

Nnc=  $3. \text{ an} = 0.050 \text{ bn} = 0.000 \text{ L} = 0.000 \text{ -} = 0.000$ 

Noc= 8. ao=  $1.000 \text{ bn} = 1.000 \text{ L} = 16.000 \text{ x0} = .000 \text{ Theta} = 90.000$ 

PACES ALONG AXE X1

1 40 0.375 DLU= 15.00 DLSU= 15.0000

PACES ALONG AXE X2

```
 1 60 0.13333 DLU= 8.00 DLSU= 8.00
```
CINEMATIC BOUNDARY CONDITION



ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179

A peer reviewed journal

#### DISTIBUTED LOAD ON A SURFACE



1 2 0 40 8 0 60 5

#### **TABLE 2 FORCE AT DISTANCE Y= 0M ALONG ALPHA LINE**





Stadium Roof Structure without Bracing and Uniform Thickness of Shell Model and Deformed Shape in Sap2000

#### **TABLE 3 MODELLING DETAILS OF ROOF STRUCTURE WITHOUT BRACING AND UNIFORM THICKNESS**.







#### **Figure 1 Stadium Roof Structure without Bracing and Uniform Thickness of Shell in Sap 2000**

Stadium Roof Structure without Bracing and Varying Thickness of Shell Model and Deformed Shape in Sap 2000

#### **TABLE 4 DETAILS OF STADIUM ROOF STRUCTURE WITHOUT BRACING AND VARYING THICKNESS**



ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 A peer reviewed journal



#### **Figure 2 Stadium Roof Structure without Bracing and Varying Thickness of Shell in Sap 2000**

Stadium Roof Structure with Bracing and Uniform Thickness of Shell Model and Deformed Shape in Sap 2000.

#### **TABLE 5 MODELLING DETAILS OF STADIUM ROOF STRUCTURE WITH BRACING AND UNIFORM THICKNESS**



#### Asian Journal of Multidimensional Research<br>2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 ISSN: 2278-4853 Vol. 12, Issue 3, March 2023

A peer reviewed journal



Stadium Roof Structure with Bracing and Uniform Thickness of Shell Model and Deformed Shape in Sap 2000

#### **TABLE 6 MODELLING DETAILS OF STADIUM ROOF STRUCTURE WITH BRACING AND UNIFORM THICKNESS**



Asian Journal of Multidimensional Research<br>ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 Vol. 12, Issue 3, March 2023 A peer reviewed journal



**Figure 4 Stadium Roof Structure with Bracing and Varying Thickness of Shell in Sap 2000**

#### **Stadium Roof Structure Detailing and View of Different Model in Sap 2000**





Asian Journal of Multidimensional Research ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 A peer reviewed journal



**Figure 5 Bracing in roof as well as top of the stadium with Uniform Thickness of RCC Shell in Sap 2000**



**Figure 6: Bracing in roof as well as top of the stadium with Varying Thickness of RCC Shell in Sap 2000**



**Figure 7 Bracing Only on top of the stadium with uniform Thickness of shell in RCC Sap 2000**



**Figure 8 : Bracing Only on top of the stadium with Varying Thickness of Shell in RCC Sap 2000**



**Figure 9: Bracing only on top of the stadium with uniform Thickness of Steel Shell in Sap 2000**

#### **RESULTS AND DISCUSSION**

For observing structural performance using different methods the model of whole superstructure of stadium is modeled in Sap2000 (clause 2.5.2.2 to Clause 2.5.2.14) and analyse result are obtained and Para sine and Dome Part is coded in to the already build up program FORTRAN (clause 2.5.2.1 and Annex I ) and analyse results are obtained then the output results are compared (clause 3.1 to 3.5).

For observing structural parameters the shell structure in sap2000 as well as FORTRAN are observe specific ultimate parameters subjected to gravity load.

For study structural parameters of roof shell structure models with varied and uniform thickness are modeled (Clause 2.5.2.16 to clause 2.5.2.24) then analsyed and the result are compared with structural parameters.

For observing structural performance shell roof structure with stiffeners and without stiffened bracing the deformation of the critical joint in the shell roof structure is obtained (clause 3.1 &

3.2) and bracing at the top of the roof (clause 3.3) is analysed to obtained the deformation of the critical joint is obtained then the results are compared to achieve permissible deflection.

Using FORTRAN complex, sap2000 and with manual verification (IS 456:2000 clause 23.2 span/350 or 20mm whichever is less) deviation in results are seen due to effect of methodologies empirical formulas and discontinuities of curvature under consideration. However, it is noted that not peak deviation is occurred while using various methods.

Stress goes increasing at the base of the dome and para sine part so contour act the stress variation of thickness of the slab is done for getting the structural performance. Also dead and lateral loads are decreased due to the thickness of the slab which ultimately decrease the permissible deflection of the tip of the stadium roof.

At the junction of roof and super structure and intersection of para sine and dome of the stadium stress concentration is maximum, to contour act this thickness of slab is vary.

#### **Comparison Base Reaction of Four Models**



#### **TABLE 8 BASE REACTIONS DUE TO GLOBAL FZ (KN)**





#### **TABLE 9 BASE REACTIONS DUE TO GLOBAL FX (KN)**



#### **TABLE 10 BASE REACTIONS DUE TO GLOBAL F<sup>Y</sup> (KN)**





ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 A peer reviewed journal



#### **TABLE 11 BASE REACTIONS DUE TO GLOBAL M<sup>Z</sup> (KN-M)**



#### **TABLE 12 BASE REACTIONS DUE TO GLOBAL M<sup>X</sup> (KN-M)**









#### **TABLE 13 BASE REACTION DUE TO GLOBAL MY (KN-M)**



#### **Comparison Displacement of Four Models TABLE 14 DISPLACEMENT U3 (M) DUE TO DEAD LOAD**



ISSN: 2278-4853 Vol. 12, Issue 3, March 2023

A peer reviewed journal





#### **TABLE 15 DISPLACEMENT U1 (M) DUE TO EQX**





#### **TABLE 16 DISPLACEMENT U2 (M) DUE TO EQY**





#### **TABLE 17 DISPLACEMENT U3 (M) DUE TO LIVE LOAD**

ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 A peer reviewed journal



### **Comparison of Displacement of Four Models with Bracing at the Top TABLE 18: DISPLACEMENT U3 (M) DUE TO COMBINATION OF DEAD AND LIVE LOAD**





ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 A peer reviewed journal



#### **TABLE 19: DISPLACEMENT U3 (M) DUE TO DEAD LOAD**



#### **TABLE 20: DISPLACEMENT U3 (M) DUE TO LIVE LOAD**

Displacement U3 (m)	<b>Without Bracing</b> and Unifrom	<b>Without Bracing</b>	With Bracing and Unifrom	With Bracing and
due to Live Load		and Varying		Varying
	Thickness	Thickness	Thickness	<b>Thickness</b>
Joint 250	$-0.01737$	$-0.016675$	$-0.01798$	$-0.01798$
Joint 263	$-0.018054$	$-0.017349$	$-0.018689$	$-0.018689$
<b>Joint 3924</b>	$-0.017294$	$-0.016657$	$-0.018006$	$-0.018006$
<b>Joint 3925</b>	$-0.016657$	$-0.016009$	$-0.017331$	$-0.017331$
<b>Joint 3934</b>	$-0.016549$	$-0.015883$	$-0.017266$	$-0.017266$
<b>Joint 7508</b>	$-0.017369$	$-0.016751$	$-0.018081$	$-0.018081$
<b>Joint 7509</b>	$-0.018054$	$-0.017429$	$-0.018795$	$-0.018795$
<b>Joint 7746</b>	$-0.017294$	$-0.016752$	$-0.018126$	$-0.018126$
<b>Joint 7747</b>	$-0.016657$	$-0.016099$	$-0.017446$	$-0.017446$
Joint 7756	$-0.016549$	$-0.015993$	$-0.017401$	$-0.017401$

https://tarj.in

ISSN: 2278-4853 Vol. 12, Issue 3, March 2023

A peer reviewed journal





#### TABLE 21: DISPLACEMENT U1 (M) DUE TO  $E_{OX}$





#### **TABLE 22: DISPLACEMENT U2 (M) DUE TO EQY**

**Comparison of Displacement of FORTAN and Model with Bracing and Uniform Thickness**



A peer reviewed journal

Table 23: Comparison of Displacement Result along Sine Part Due to Dead Load of FORTAN and Sap Model with Bracing and Uniform Thickness





Table 24: Comparison of Displacement Result along Para Part Due to Dead Load of FORTAN and Sap Model with Bracing and Uniform Thickness



Table 25: Comparison of Displacement Result along Sine Part Due to Live Load of FORTAN and Sap Model with Bracing and Uniform **Thickness** 





**Joint** 7509

#### Asian Journal of Multidimensional Research ISSN: 2278-4853 Vol. 12, Issue 3, March 2023 SJIF 2022 = 8.179 A peer reviewed journal

Table 26: Comparison of Displacement Result along Para Part Due to Live Load of FORTAN and Sap Model with Bracing and Uniform Thickness





Comparison of Displacement of FORTAN and Model without Bracing and Uniform Thickness of Steel Plate

Table 27: Comparison of Displacement Result Due to Dead Load of FORTAN and Sap Model without Bracing and Uniform Thickness of Steel Plate





A peer reviewed journal

Table 28: Comparison of Displacement Result Due to Live Load of FORTAN and Sap Model without Bracing and Uniform Thickness of Steel Plate





#### **DISCUSSION**

Form the result obtained above, the following observation was made:

Discontinuous function is not calculated by sap2000 and FORTAN complex only perform by elastic theory approach. Due to this the variation of results occurs greater as we aspect.

#### **Discussion no 1.**

#### **Stadium Roof Structure without Bracing Uniform Thickness of shell, without bracing Varying Thickness of Shell, with bracing uniform thickness of shell and with bracing varying thickness of shell Model**

Through comparison of displacement obtained by different models of roof structure, the displacement of the critical point of the roof is over the permissible displacement.

#### **Discussion no 2.**

#### **Stadium Roof Structure with bracing at the top of roof in four model without Bracing with Uniform Thickness of shell, without bracing and Varying Thickness of Shell, with bracing and uniform thickness of shell and with bracing and varying thickness of shell Model**

Through comparison of displacement obtained by different models of roof structure, the displacement of the critical point of the roof is in the limit of permissible displacement.

#### **Discussion no 3.**

#### **Stadium Roof Structure model bracing with Uniform Thickness of shell and FORTRAN**

Through comparison of displacement obtained by models of roof structure and FORTRAN, the displacement of the critical point of the roof are observed due to adopting continuity by manual and FORTRAN complex are observed not exceeding permissible limit of deflection.

#### **Discussion no 4.**

**Stadium Roof Structure model without bracing and Thickness steel plate of shell and FORTRAN** 

Through comparison of displacement obtained by models of roof structure without bracing and thickness steel plate and FORTRAN, the displacement of the critical point of the roof different deflections are observed for bracing system and material assigned converting RCC shell roof in to steel.

Final Real Stadium with dome as well as para sine parts

Using sap2000 and getting the results in FORTAN (specific parts) following outputs are achieved

- 1) In intersecting line of dome and para-sine stress concentration seen but rectified using connecting members.
- 2) The permissible limit of deflection is achieved by connecting peak of para sine.
- 3) Different deflections are observed for bracing system and material assigned converting RCC shell roof in to steel.

#### **CONCLUSION**

- The varying thickness of RCC shell has important rule to minimize tip deflection up to permissible limit, stress concentration and stiffness through bracing system of shell structure used in roof of stadium.
- The para sine form Mongue's surface curved shell roofs with super structure intersected to the adjacent dome structure are found stable in both gravity and lateral loads during analysis.
- The considerable alternation in different adapted methodology to achieve structural parameters of roof shell structure having uniform and varying thickness are observed due to adopting continuity by manual and FORTRAN complex are observed not exceeding permissible limit of deflection.
- The permissible deflection undergo by different kinds of load in shell roof structure is achieved with lateral, diagonal stiffeners at the roof top and bracing within shell structure.
- The intersection portion of dome and para sine should be braced by using stiffener to overcome stress concentration in intersection line of those connect parts of dome and para sine.

#### **REFERENCES:**

- **1.** Laith N. Hussain, Ahlam S. Mohammed, Ahmed A. Mansor (2020): Finite element analysis of large-scaled reinforced concrete shell of dome. Journal of Engineering Science and Technology Vol. 15, No. 4 (2020) 2712 - 2729 © School of Engineering, Taylor's University
- **2.** Wei Li, Anzong Zheng, Lihua You, Xiaosong Yang, Jianjun Zhang and Ligang Liuy (2017): Ribbed shell structure. Pacific Graphics 2017 J. Barbic and O. Sorkine-Hornung (Guest Editors) Volume 36 (2017), Number 7
- **3.** Lamichhane GP (2018): Complicated features and their solution in analysis of thin shell and plate structures. 2018. 14 (6). 509–515 structural mechanics of engineering constructions and buildings http://journals.rudn.ru/ structural-mechanics.
- **4.** SS bhabikatti (2005): Finite element analysis
- **5.** Eduard ventsel and Theodor Krauthammer (2001): Theory of plate and shell. ISBN: 0-8247- 0575-0
- **6.** Azhar Mahmood Nasir (2002): Axisymmetric shell structure for multi-use (Doctoral Dissertation).
- **7.** OstovariDailamani, S. (2010): Behaviour of cylindrical and doubly curved shell roofs under earthquake (Doctoral dissertation).
- **8.** Attia Mousa and Hesham El Naggar (1991): Finite Element Analysis of Polygon Shaped Shell Roof. Journal of Civil Engineering and Architecture 11 (2017) 420-432 doi: 10.17265/1934-7359/2017.05.002
- **9.** Hamadi, D., Ayoub, A. and Abdelhafid, O. (2016). A new flat shell finite element for the linear analysis of thin shell structures. European Journal of Computational Mechanics, 24(6), pp. 232-255. doi: 10.1080/17797179.2016.1153401
- **10.** Djamal Hamadi, Oussama Temami, Abdallah Zatar, Sifeddine Abderrahmani [2014]: A Comparative Study between Displacement and Strain Based Formulated Finite Elements Applied to the Analysis of Thin Shell Structures. World Academy of Science, Engineering and Technology International Journal of Civil, Architectural, Structural and Construction Engineering Vol:8 No:8, 2014
- **11.** Kalins and D.A. Goderfy (1973): Seismic analysis of thin shell structure
- **12.** Mariya Jacob, Aswathi Mohanan (2017): Study the Effect of Wind Load and Dead Load on RC Hyperbolic Cooling Tower by the Provision of Stiffeners. IJISET - International Journal of Innovative Science, Engineering & Technology, Vol. 4 Issue 4, April 2017 ISSN (Online) 2348 – 7968 | Impact Factor (2016) – 5.264
- **13.** Aliyu, Musa Dahiru (2013): The Dynamic Response of Cylindrical Roof Shell under the Effect of Direct Damping Model. American Journal of Engineering Research (AJER) e-ISSN : 2320-0847 p-ISSN : 2320-0936 Volume-02, Issue-12, pp-350-359 [www.ajer.org](http://www.ajer.org/)
- **14.** Kanta (2015). Of thin concrete shell roof. Civil Engineering and Geosciences. Delft University of Technology.
- **15.** Yi Zhou, Yuanqi Li, Yingying Zhang and Akihito Yoshida (2018). Characteristics of Wind Load on Spatial Structures with Typical Shapes due to Aerodynamic Geometrical Parameters and Terrain Type. Hindawi Advances in Civil Engineering Volume 2018, Article ID 9738038, 18 pages<https://doi.org/10.1155/2018/9738038>
- **16.** Rynkovskaya (2017): Carved mongue surface as new forms in architecture. MATEC Web of Conferences 95, DOI: 10.1051/matecconf/201795 ICMME 2016 17006 (2017) 17006
- **17.** Shadi Ostovari Dailamani (2010): Behavior of Cylindrical and Doubly-Curved Shell Roofs under Earthquake.

A peer reviewed journal

- **18.** V.N Ivanov (2017): Analysis of Thin Walled Wavy Shell of Monge Type Surface with Parabola and Sinusoid Curves by Variational-Difference Method. MATEC Web of Conferences 95, DOI: 10.1051/matecconf/201795 ICMME 2016 12007 (2017) 12007
- **19.** António Rui Fernandes Solheiro Institute Superior Técnico, Lisbon, Portugal (2017): Finite element analysis of shell structure.
- **20.** American Society of Civil Engineers New York, N.Y.: The Society (1952): Design of Cylindrical Concrete shell roofs/ prepared by the Committee on Masonry and Reinforced Concrete of the Structural Division, through its Subcommittee on Thin Shell Design. http:/hdl.handle.net/2027/wu.89078515517